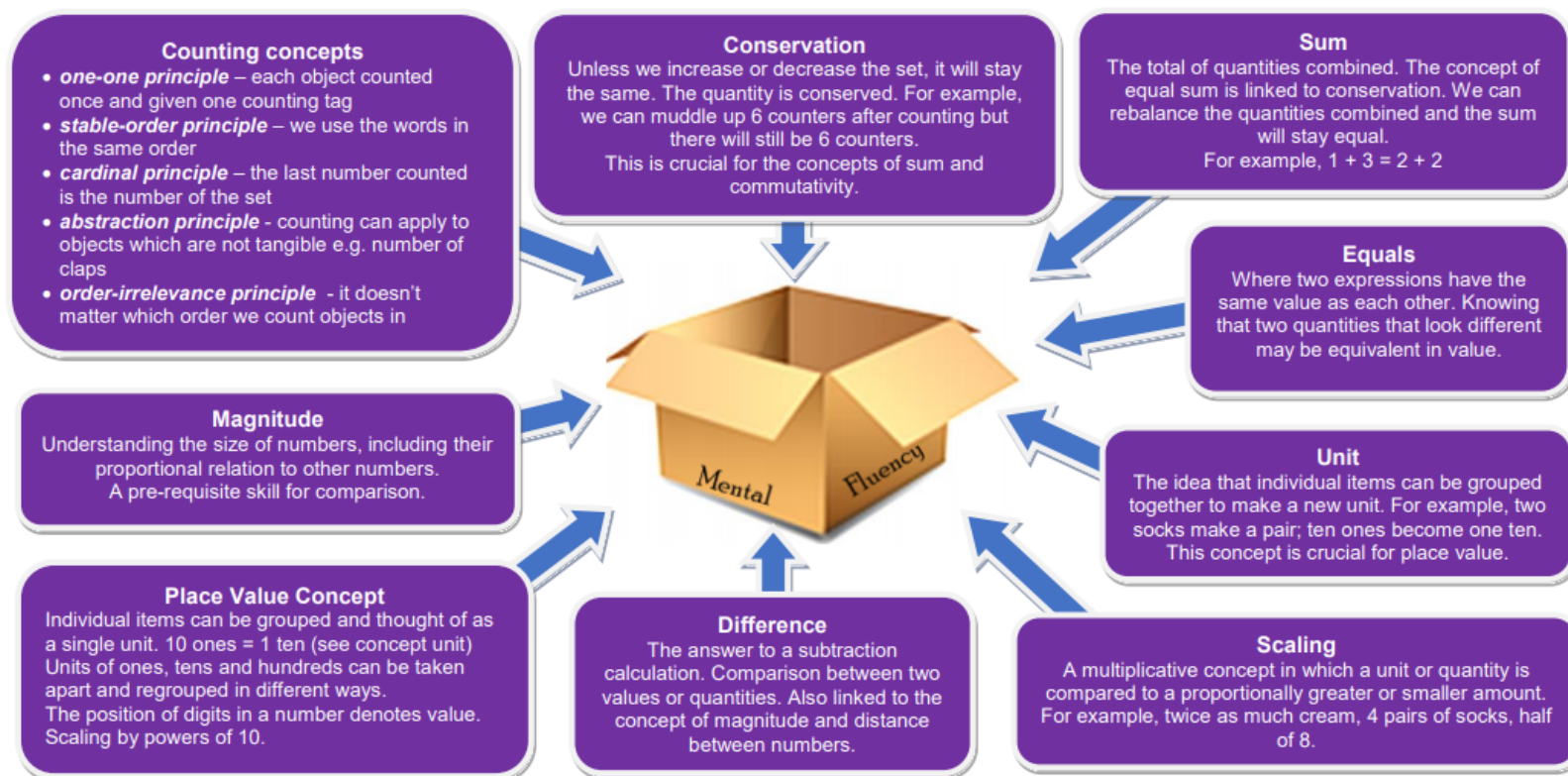


Robin Hood Primary School Fluency progression map 2022-23

The NCETM set out 5 big ideas for mastery: **coherence**, **representations**, **variation**, **mathematical thinking** and **fluency**. They state that fluency demands more of students than **memorisation** of a single procedure or collection of facts. It encompasses a mixture of **efficiency**, **accuracy** and **flexibility**. **Quick and efficient recall** of facts and procedures is important in order for students to **think strategically** and **solve problems**. Fluency also demands the **flexibility** to move between **different contexts** and **representations** of mathematics, to **recognise relationships** and **make connections**, and to make appropriate choices from a **whole toolkit of methods, strategies and approaches**. This document aims to provide a structure in which teachers will explicitly teach these in a coherent and well thought out manner. The core mathematical concepts children need to become fluent are:



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In order to achieve these, they will have to master the following skills:

Subitising	the ability to see number as pattern, such as dice patterns. This supports pupils to see numbers within numbers and better regrouping (partitioning).
Regrouping (partitioning)	the ability to break numbers up and recombine them flexibly
Counting on and counting back	in a variety of interval steps
Reordering	knowing when and how to reorder to make calculations easier
Finding complements	links to reordering, identifying useful complements pairs or trios of 1, 10, 60 etc.
Applying the inverse	use of fact family knowledge to 'undo'
Rounding	to a range of benchmark numbers
Estimation	both linear estimation on number lines and scales, and of quantities and calculations to support an increasing sense of what is reasonable
Compensation	to use rounding to add or subtract too much or too little and adjust accordingly
Rebalancing	to adjust the parts of addition and subtraction facts to make a calculation easier
$\times \div$ by powers of 10	
Doubling and halving	
Rearranging	to adjust the groups in multiplication and division to make a calculation easier

These are broken down below into skills which each year group should focus on. Below this are the non-negotiable key skills, which each child should leave the year group knowing fluently.

Children should be encouraged to regularly use, compare and evaluate the efficiency of different methods.

DEFINITIONS

Arithmetic equations and their parts

Addition equation

$$\begin{array}{r} 2 \quad 5 \\ + 1 \quad 1 \\ \hline 3 \quad 6 \end{array}$$

← addend
← addend
← sum

Subtraction equation

$$\begin{array}{r} 2 \quad 5 \\ - 1 \quad 1 \\ \hline 1 \quad 4 \end{array}$$

← minuend
← subtrahend
← difference

Multiplication equation

$$\begin{array}{r} 3 \\ \times 5 \\ \hline 15 \end{array}$$

← factor
← factor
← product

Division equation

$$\begin{array}{c} \text{divisor} \\ \downarrow \\ \text{dividend} \rightarrow 12/4 = 3 \leftarrow \text{quotient} \\ \downarrow \\ \text{divisor} \\ \downarrow \\ \text{dividend} \rightarrow 12 \div 4 = 3 \leftarrow \text{quotient} \\ \text{quotient} \rightarrow 3 \\ \text{divisor} \rightarrow 4 \overline{)12} \leftarrow \text{dividend} \end{array}$$

The Commutative Law

The Commutative Law says that when you add or multiply numbers, you get the same answer if you swap the numbers round.



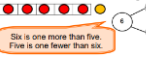
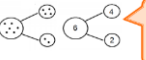
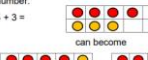
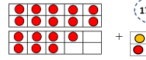
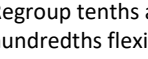
$$6 + 3 = 9 = 3 + 6$$


$$4 \times 2 = 8 = 2 \times 4$$

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Fluency skill	F2	1	2	3	4	5 and 6
Subitising	Recognise groups up to 5 without the need to count Identify 5 and use as a benchmark number e.g. Numbers 6 and 7 where 5 is the benchmark i.e. 6 is 1 more than 5 using five frames and additional counters.  Ensure transference to fingers.  7 fingers can be shown by 5 fingers and 2 more fingers.	Recognise groups (up to 5) without the need to count and use this to identify numbers up to 10  I can see three and three and one makes seven. Four and one and one and one makes seven. (through the use of magnetic trays and ten frames)				

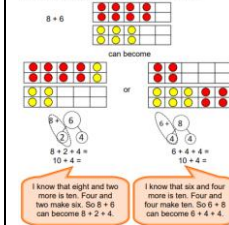
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	Identify numbers within a whole set e.g.  I can see 3 and 3 and 1. I can see 4 and 1 and 1 and 1. I can see 4 and 3.					
Regrouping (partitioning)	Use 5 as a benchmark number Think 5 Where the whole is 6 or 7 and one of the parts is 5 (to secure benchmark from 5).  Understand a whole = part and part  Identify a group as a unit e.g. a unit is 2 teddies 	'Think 10' – able to partition a number into 10 and some more e.g.  Able to regroup a whole up to 10 into different parts and understand the commutativity of this Able to use 5 as a benchmark for regrouping for addition up to 10 e.g. Think 5 for addition using five as a benchmark number. 	Regroup two digit numbers flexibly and in multiple ways e.g.  Able to 'think 10' for addition e.g. $\square = 17 + 8$ a) Regrouping the second addend  b) Regrouping the first addend 	Regroup three digit numbers flexibly and multiple ways e.g. Using part whole models, regroup 3-digit integers flexibly and in multiple ways.  Regroup for addition to allow bridging through 10 and 100. Work flexibly and reason about the most efficient methods e.g.  This can be applied to regrouping addends in 3-digit + 1-digit calculations e.g. $247 + 8$.  This can also be applied to regroup to bridge through multiples of 100 e.g. $70 + 50$ or $460 + 80$.  Regroup for subtraction to allow bridging through 10 and 100. Work flexibly	Regroup four digit numbers flexibly and in multiple ways Regroup tenths and hundredths flexibly and in multiple ways e.g.  In addition, regroup to 'think 100' with more complex 3 digit addends e.g.  In subtraction, regroup to 'think 100' with more complex 3 digit numbers Use regrouping strategies to fractional part wholes, as well as other measures such as time and money e.g.	Use regrouping as a valid method in a multi-step problem e.g.  Regroup for multiplication in a variety of ways e.g. 24  Regroup for division in a variety of ways e.g. $72 \div 3$

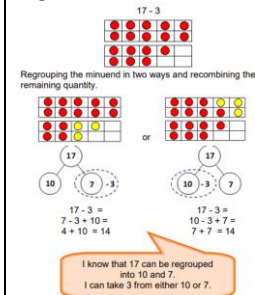
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Able to use 10 as a benchmark for regrouping for addition up to 20 (think "10 and some more") e.g.

Regrouping numbers to 20 leading to 'think 10 for addition'. Pupils should experience regrouping either addend.



Able to use 10 as a benchmark for regrouping for subtraction up to 20, using wither the minuend or the subtrahend, without bridging through ten e.g.



Able to use 10 as a benchmark for regrouping for subtraction up to 20, using either the minuend or the

Able to 'think 10' for subtraction e.g.

Exploring that either the minuend or the subtrahend can be regrouped.

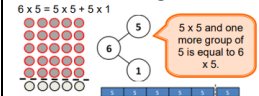
25 - 13 = 12



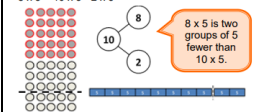
Regrouping the subtrahend - normally to a multiple of ten.



'Think 5' for multiplication and division e.g.



Think 10 for multiplication and division

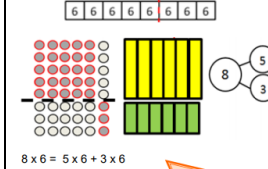


with both the minuend and the subtrahend.

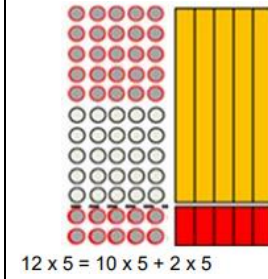
In multiplication, regroup to the '5' benchmark, working flexibly to regroup either the multiplier or the multiplicand e.g.

Application of the distributive law.

Regrouping the multiplier (number of groups) e.g.



In multiplication, regroup to the 10 benchmark working flexibly to regroup either the multiplier or the multiplicand e.g. 12 x 5

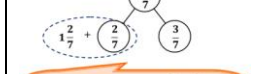


For example: $\frac{4}{7} + \frac{5}{7} = 1$

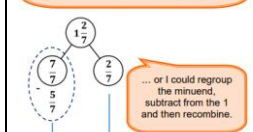
Both addends can be regrouped using complements to 1 and 'some more'.



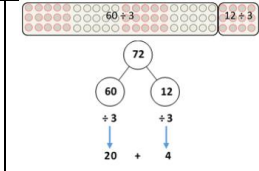
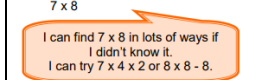
For example: $1\frac{2}{7} - \frac{5}{7} = \frac{4}{7}$



I can regroup the subtrahend $\frac{5}{7}$ into $\frac{2}{7}$ and $\frac{3}{7}$. Then I can take away the $\frac{2}{7}$ leaving $\frac{4}{7}$ or 1 and finally take away $\frac{3}{7}$.

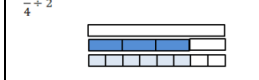
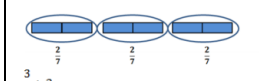


Use regrouping methods to find unknown products in multiplication e.g.



Regroup for division of fractions by whole numbers e.g.

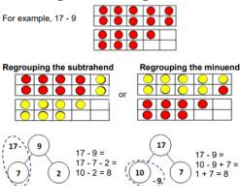
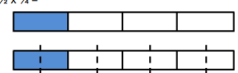
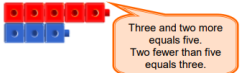
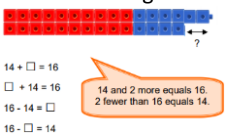
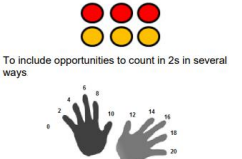
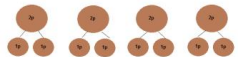
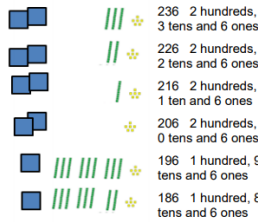
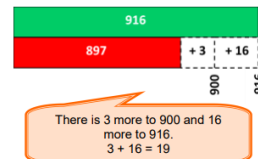
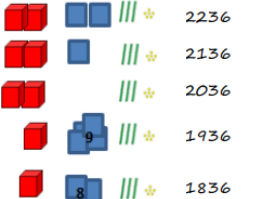
I know that 12 ÷ 3 can be thought of as 'If I share 12 equally between 3 groups, how many in each group?'



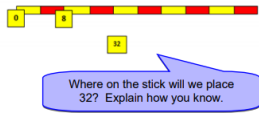
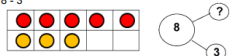
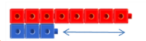
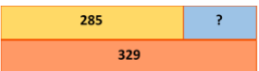
$\frac{3}{4} + 2$ can be understood as: "If I share $\frac{3}{4}$ equally between 2 groups, how many in each group?"

Regroup fractions for multiplication (focus on this understanding before

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		subtrahend, bridging through ten e.g. For example, $17 - 9$  Regrouping the subtrahend or Regrouping the minuend Nine can be regrouped into 7 and 2. I can take 7 from 17 to leave 10 and then I can use my number bonds to take away 2 more. Seventeen can be regrouped into 10 and 7. Then I can use my number bonds to take 9 from 10. I'm left with 1. Then I add one to seven.			applying the rule) e.g. I know that 3×4 could mean 3 groups of 4. So $\frac{1}{2} \times \frac{1}{4}$ means half a group of $\frac{1}{4}$. $\frac{1}{2} \times \frac{1}{4} =$  When we find half of any number, we divide it by two. The blue part has a value of $\frac{1}{4}$. When I halve it, it makes 8.
Counting on and back	Be able to count fluently. To do this, children need to have mastered: The one-one principle – each object is counted once and given one counting tag The stable-order principle – we use the words in the same order The cardinal principle – the last number counted is the number of the set The abstraction principle - counting can apply to objects which are not tangible e.g. number of claps The order-irrelevance principle - it doesn't matter which order	Count on to find the total and difference e.g.  Three and two more equals five. Two fewer than five equals three. Count on to find the total and difference and link this knowledge to fact families e.g.  14 + 2 = 16 16 - 2 = 14 14 + 2 = 16 16 - 2 = 14 Be able to skip count in a variety of ways to promote the 2x tables and doubles e.g. Counting groups of objects with two hands (drawing out understanding of doubles).  To include opportunities to count in 2s in several ways 	Count in units where units are different e.g. 36 = ten, twenty, thirty, one, two, three, four, five, six Count on and back from any two digit number and notice what changes and doesn't e.g.  34 3 tens and 4 ones 44 4 tens and 4 ones 46 4 tens and 6 ones 36 3 tens and 6 ones 26 2 tens and 6 ones I can see that the tens are changing but the ones are staying the same. Skip count in 3's in a variety of ways, forwards, backwards and from different starting points. Count on to find complements to	Count on and back from any three digit number and notice what changes and what doesn't e.g.  236 2 hundreds, 3 tens and 6 ones 226 2 hundreds, 2 tens and 6 ones 216 2 hundreds, 1 ten and 6 ones 206 2 hundreds, 0 tens and 6 ones 196 1 hundred, 9 tens and 6 ones 186 1 hundred, 8 tens and 6 ones Count on to find complements to benchmark numbers within 1000 e.g. 916 - 897.  There is 3 more to 900 and 16 more to 916. $3 + 16 = 19$ Understand the connections between the 3, 4 and 8 times tables and know strategies to be	Count on and back from any four digit number and notice what changes and what doesn't e.g.  2236 2 thousands, 2 hundreds, 3 tens and 6 ones 2136 2 thousands, 1 hundred, 3 tens and 6 ones 2036 2 thousands, 0 hundreds, 3 tens and 6 ones 1936 1 thousand, 9 hundreds, 3 tens and 6 ones 1836 1 thousand, 8 hundreds, 3 tens and 6 ones Count on and back in multiples and make counting connections e.g. counting in 6's, 60's, 600's, 0.6's Count in 25's, 50's, 0.1's and 0.001's Skip count all the times tables and understand the connections between them  If I know $x1, x2, x5, x10$, what else can I work out? 1 more, 1 less $x4 \cdot x8 \cdot x9 \cdot x3$ 2 more, 2 less $x7 \cdot x6 \cdot x4 \cdot x3$

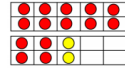
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	we count objects in Be able to count on when an addend is given, rather than count all Be able to identify the largest number and count on from it	Be able to skip count in 5s and 10s in a variety of ways, forwards, backwards and from different starting points.	benchmark numbers within 100 e.g. Drawing out complements to benchmark numbers. 	able to work out unknowns e.g. 		
Reordering and finding complements		Reorder to ensure efficient counting e.g. There are 6 animals.  How many different ways can you sort the animals?	Reorder numbers to find complements when adding three one digit numbers e.g. 6+7+4 (add the 6 and 4 first to make 10)	Reorder three or more numbers up to 1000 to find complements e.g. 75+95+25 can be reordered into 75+25 to make the benchmark 100, then add 95 to total 195. Or 6+9+4+5+1 (reorder to make number bonds to 10)	Reorder three or more numbers up to 10,000 to find complements e.g. 800+240+360 310+700+30 = Reorder three or more numbers involving tenths and hundredths to find complements e.g. 1.5+3+0.5 2.5+25+5+2.5= (reorder to make wholes)	Reorder three or more numbers to find complements where the arrangement is more complex e.g. £3.99+£7.80+£2.01
Applying the inverse		Think addition to solve subtraction with numbers to 10 e.g. 8 - 3    Think addition to solve subtraction with	Think addition to solve subtraction with numbers up to 100 e.g. Tens Ones - Ones = without regrouping  $27 - \square = 4$ $4 + \square = 27$ Understand the relationship between multiplication and division. In multiplication, understand the interrelationship between multiplier, multiplicand	Think addition to solve subtraction with numbers up to 1000 e.g.  $329 - 285 = \square$ so $285 + \square = 329$		

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numbers up to 20 e.g.

$$16 - 2 = \square$$



I can see that sixteen can be split into fourteen and two.

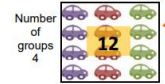
I know that fourteen and two more is sixteen. So 16 subtract two is fourteen.

and product. In division, understand the relationship between the dividend, divisor and quotient e.g.

$$4 \times 3 = 12$$



Number in each group
3



$$4 \times 3 = 12$$

$$3 \times 4 = 12$$

$$12 \div 3 = 4$$

$$12 \div 4 = 3$$

$$12 \div 3 = 4$$



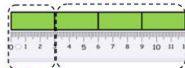
I can see that 3 can be taken from 12, four times.



I can see that 12 can be shared into 4 equal groups with 3 in each group.

I know that I can use $4 \times 3 = 12$ to answer $12 \div 3$ or $12 \div 4$.

Make the connections between multiplication and division and fractions e.g.



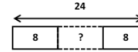
I can see a quarter of 12 is equal to 3 and three quarters of 12 is equal to 9.



One third of 12 equals 3. Two thirds of 12 is 9.

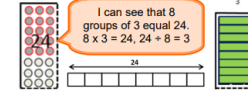
sharing e.g.

By grouping



I can see that 3 groups of 8 equal 24. $3 \times 8 = 24$, $24 \div 8 = 3$

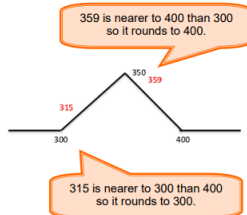
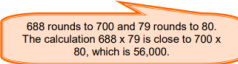
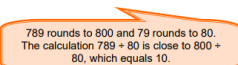
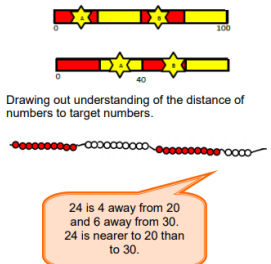
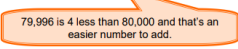
By sharing



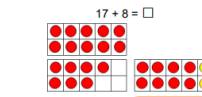
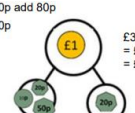
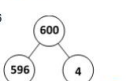
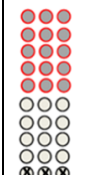
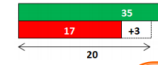
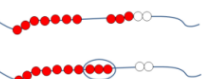
I can see that 8 groups of 3 equal 24. $8 \times 3 = 24$, $24 \div 8 = 3$

Make further connections between multiplication and division and fractions

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Rounding				Identify the midpoint between a set of numbers under 1000 (and use this in order to understand rounding) e.g. 	Round to the nearest 10, 100, 1000 and other units such as money and time	Round to the nearest 10, 100, 1000, 10,000 and other units such as money, time, decimal numbers, negative numbers Use rounding as an estimation for multiplication and division e.g. $688 \times 79 =$  $789 \div 79 =$ 
Estimation			Estimate the distance of numbers from target numbers under 100 e.g. 	Estimate the distance of numbers from target numbers under 1000 to prepare for rounding e.g. 234 is 4 from 230 and 6 from 240. 240 is nearer to 230 than 240	Estimate the distance of numbers from target numbers up to 10,000, including tenths and hundredths to prepare for rounding e.g. 2134 is 34 from 2100 and 66 from 2200. 2134 is nearer to 2100 than 2200.	Estimate the distance of numbers from target numbers up to 1,000,000, including decimal numbers and negative numbers, to prepare for rounding e.g. 20,034 is 4 from 20,030 and 6 from 20,040. 20,034 is nearer to 20,030 than to 20,040.
Compensation			'Think 10', use benchmark numbers and compensate	Use benchmark numbers and compensate for adding and subtracting numbers up to 1000,	Use benchmark numbers and compensate for adding and subtracting numbers up to 10,000, including money and time e.g. "I could think of $2550 + 490$ as compensation because adding 490	Use number knowledge to look for 'nearly numbers' in calculations (including decimals) e.g. $7834 + 79,996$ 

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			for trickier calculations e.g. $17 + 8 = \square$  Adding 8 is like adding ten and taking 2 away. Subtracting 8 is like subtracting ten and adding 2 back. Apply this to subtraction.	including money e.g. £3 and 40p add 80p £3 and 40p  Adding 80p is the same as adding £1 and subtracting 20p. 632 - 596  Subtracting 596 is the same as subtracting 600 and adding 4 back. Use known facts to compensate for unknown multiplication and division calculations up to 12x tables e.g. $9 \times 3 = 10 \times 3 - 3$ $9 \times 3 = 10 \times 3 - 1 \times 3$  Nine groups of three is equal to 10 groups of three, less 1 group of 3.	is like adding 500 and taking ten away. Now my calculation looks like this: $2550 + 500 - 10 = 3040$.  Adding 50 minutes is like adding one hour and taking away 10 minutes.  Subtracting £17.00 is like subtracting £20.00 and adding back £3.00. Compensate in multiplication and division with numbers up to 1000 e.g. $3 \times 9 = 3 \times 10 - 3$  Nine groups of three is equal to ten groups of three, less 1 group of 3. I could use this to find 90×3. $100 \times 3 - 10 \times 3$	$132,457 - 11,999 =$ Subtracting 11,999 is like subtracting 12,000 and then adding 1. Now my calculation is $132,457 - 12,000 + 1 =$
Rebalancing			Understand the concept of equal sum (that the sum remains equal when the addends are rebalanced in addition) with numbers up to 20 e.g.  I can prove that $7 + 5 = 10 + 2$ using a bead string.	Use the equal sum concept with numbers up to 1000 as a method to solve addition calculations e.g. e.g. $52 + 37$  I move 2 beads from the 52 and give them to the 37. Now I can solve $50 + 39$. It's easier. Use the equal difference concept with numbers up to 1000 as a method to	Use the equal sum concept with numbers up to 10,000, including units of time and money, as a method to solve addition calculations e.g. $255 + 49$ is easier if I take one from the 255 and give it to the 49. My sum stays equal. Then my sum becomes $254 + 50 = 304$.	Apply the equal sum concept to a range of numbers and missing number problems (including units of time and money) e.g. $24 + \square = 30 + 3$. $39 + 52$ $345 + 198$ $0.39 + 6.54$ $5.1 + 2.7 = \square + 4.8$ $7834 + 79,996$ 79,996 is 4 away from 80,000. I can rebalance the sum by taking 4 from 7834 and giving it to the 79,996. Now I have $80,000 + 7,830 = 87,830$.

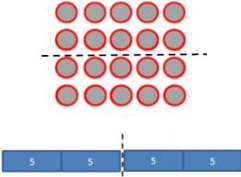
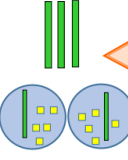
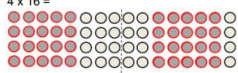
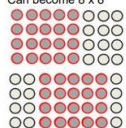
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			Understand the concept of equal difference (subtracting the same quantity from both subtrahend and minuend maintains the difference) with numbers up to 20 e.g. 5 - 3 is equal to 7 - 5 5 - 3 is equal to 3 - 1 If I wanted to solve 21 - 16, I can take 1 from each number and solve it as 20 - 15. That is an easier calculation.	solve subtraction calculations e.g. 25 13 12 10 30 18 I can take 3 from each number and the difference will remain equal. I can add 5 to each number and the difference will remain equal. If I give 10 minutes from the 1 hour 44 to the 50 minutes then I can add on 1 hour. Use the equal difference concept with numbers up to 10,000, including units of time and money as a method to solve subtraction calculations e.g. 187 56 191 60 181 50 I can add 4 to each number and the difference will remain equal. I can take 6 from each number and the difference will remain equal. Which strategy did you prefer? Explain why. Use equal difference concept with tenths and simple fractions e.g. 6.4 - 3.9 6.6 - 3.2 7.7 - 4.8 $1\frac{2}{7} - \frac{8}{7}$	Use the equal difference concept with a range of numbers, decimals and fractions e.g. 132,457 - 11,999 = 11,999 is nearly 12,000. If I add one to each number the difference will stay equal. Now my calculation is 132,458 - 12,000 = $\square = 4 - 1.15$ 4 1.15 3.85 1 It is easier if I subtract 0.15 from each number. The difference will stay the same. Now my calculation is 3.85 - 1 = £122.56 - £87.99 9.1 - 6.7 15.3 - 5.7
X ÷ by powers of 10			Understand the concept of x and ÷ 10, and use known facts to multiply and divide by 10 and 100 e.g. I know that when multiplying 3 by 40, 40 is ten times bigger than 4, so my answer will be ten times bigger than 3 x 4	Understand the concept of x and ÷ 10, and use known facts to multiply and divide by 10, 100 and 1000 e.g. 4000 x 6, 240 ÷ 4, 750mm = _____ cm.	X and ÷ by powers of 10, including 2 step problems. Includes decimals e.g. The division diagram shows $7200 \div 200 = 36$. Use the diagram to solve: 7200 ÷ 200 = $\square$ 18,000 ÷ 200 = $\square$ 5,400 ÷ $\square$ = 27 $\square$ = 6,600 ÷ 200 5600 ÷ 80 30 = $\square$ ÷ 12 270 ÷ 9 = $\square$ ÷ 0.9 7 x 0.001 1.8 ÷ 0.1 3.25 ÷ 0.00001 Circle two numbers that multiply together to equal 10 million 200 2,000 5,000 50,000 "I know that 10 million

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				23 10 23 groups of ten. 20 groups of ten is equal to 200. 3 groups of ten is equal to 30. 23 groups of 10 is equal to 230. $\square = 120 \div 3$ 120 is 12 tens. 12 tens divided into 3 groups is equal to 4 tens. 4 tens is 40. So $40 = 120 \div 3$.	has 8 place values columns and 7 0's. I know that $2 \times 5 = 10$. This already has one 0, therefore I could use 2000 x 5000 or $200 \times 50,000$ "																				
Doubling and halving	Be able to find double of a number (up to 10) using concrete resources e.g. Outdoors Have number shapes hidden around the outdoor area. Give each child a number shape and ask them to find another one the same to make a double. Encourage them to say the double they have found, e.g. Double 5 is 10 Be able to link 'fair sharing' between 2 to the language of 'equal parts' and 'half'	Find doubles up to 20 and link this to repeated addition e.g. <table><thead><tr><th>Build</th><th>Represent</th><th>Add</th><th>Double</th></tr></thead><tbody><tr><td> </td><td> </td><td>$1 + 1 = 2$</td><td>Double 1 is 2</td></tr><tr><td> </td><td> </td><td>$2 + 2 = 4$</td><td>Double 2 is 4</td></tr><tr><td> </td><td> </td><td>$3 + 3 = 6$</td><td>Double 3 is 6</td></tr><tr><td> </td><td> </td><td>$4 + 4 = 8$</td><td>Double 4 is 8</td></tr></tbody></table> Understand the link between doubling, halving odds and evens	Build	Represent	Add	Double			$1 + 1 = 2$	Double 1 is 2			$2 + 2 = 4$	Double 2 is 4			$3 + 3 = 6$	Double 3 is 6			$4 + 4 = 8$	Double 4 is 8	Find doubles and near doubles with numbers up to 100 e.g. Finding doubles and near doubles I know that 3 add 3 makes 6. So $3 + 4$ must be 1 more. $3 + 2$ must be one less. How can we use this to add $13 + 14$, $23 + 4$ or $30 + 40$? Relate repeated addition to multiplication e.g. $3 + 3 = 2 \times 3$ Use doubling to relate multiplication facts e.g. 2×5 is equal to double 1×5.	Find doubles and near doubles with numbers up to 1000 e.g. 70 + 60 is like double 60 plus 10. It's also 10 less than double 70. Use doubling and halving to find unknown products e.g. To include 'double and double' strategy for $x8$ and halving strategy for finding $x5$. I can find 5 lots by finding 10 lots and halving the product. Be able to generalise what happens when we halve a number that is an odd multiple of 100 e.g. "If I halve 700, I can share three hundreds into each group but then I have to regroup the last hundred into ten tens. Each group will then get	Find doubles and near doubles with numbers up to 10,000. Use doubling and halving to find unknown products in multiples of 10 e.g. 9×200 "I know that $9 \times 100 = 900$, and 200 is double 100, so to find the product I can double 900 to get 1800."
Build	Represent	Add	Double																						
		$1 + 1 = 2$	Double 1 is 2																						
		$2 + 2 = 4$	Double 2 is 4																						
		$3 + 3 = 6$	Double 3 is 6																						
		$4 + 4 = 8$	Double 4 is 8																						

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			 4 x 5 is double 2 x 5. I can show it as an array and as a linear model. Be able to generalise what happens when we halve a number that is an odd multiple of 10 e.g.  If I halve 30, I can share one ten into each group but then I have to regroup the last ten into ten ones. Each group will then get five ones. So 1 ten and 5 ones in each group is 15.	five tens. So three hundreds and 5 tens in each group is 350.” “Where there is an odd multiple of ten or hundred, I will always have to regroup my last ten or hundred into the next place value column down. Then I will share half of that between the two groups which will always be 5 units (5 ones or 5 tens)”		
Rearranging				Rearrange the multiplier and multiplicand using knowledge of doubles and halves to make a calculation more manageable e.g. $4 \times 16 =$  Can become 8×8  Doubling the 4x and halving the group of 16 gives me 8×8 . The area remains equal.	Use the relationship between doubling and halving to manipulate the multiplicand and the multiplier to find more efficient calculations e.g. $12 \times 2.5 =$ $16 \times 6 \frac{1}{4} =$ $12 \times 2.5 = 6 \times 5$. I halved the 12 and doubled the 2.5 to make the calculation easier. $16 \times 6 \frac{1}{4} = 8 \times 12 \frac{1}{2} = 4 \times 25 = 100$ I can make this easier for me by doubling and doubling again the $6 \frac{1}{4}$. This means I have to halve and halve again the 16 to maintain the area. Now I get $4 \times 25 = 100$.	Use halving and halving for division, understanding why the halving needs to be done to the dividend and divisor and not the

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						quotient e.g.  $72 \div 4 = (72 \div 2) \div 2$ When I am dividing by 4, I like to halve the number and halve it again. For example, if I shared 12 cookies among 4 children each child would get 3 cookies. $12 \div 4 = 3$  I can also see that 6 cookies shared between 2 people would give the same group size. The size of the group hasn't changed. So $12 \div 4$ can be changed into $6 \div 2$.  As I am trying to find out the group size, I can also see that 3×1 gives me the group size. So $12 \div 4$ can be thought of as $6 \div 3$ and $3 \div 1$. I can see all of these in the array. Applying this conceptual understanding to larger numbers encourages playfulness with division. $364 \div 16 =$ $182 \div 8 =$ $91 \div 4 =$ $45.5 \div 2 =$ 22.75 I saw that I could halve both the dividend and the divisor, so I did to see if it made it easier. Then I realised that I could halve them again and again. Apply halving and doubling to fractions e.g. Pupils have already secured conceptual understanding of this rule, for example: $5 \times 4 = 10 \times 2 = 20 \times 1$ Apply this understanding to fractions, for example: $\frac{1}{2} \times \frac{1}{4} =$ If we double the first term and halve the second, we can transform the calculation to: $1 \times \frac{1}{8} = \frac{1}{8}$
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Fluency also means **automatic recall of key facts**. These are the facts which children should be able to recall at the end of each year group. They will need to explicitly be taught strategies (doubles and near doubles, compensating etc.) to work them out as well as lots of practice in order to achieve automaticity in recall.

	0	1	2	3	4	5	6	7	8	9	10
0	0 + 0	0 + 1	0 + 2	0 + 3	0 + 4	0 + 5	0 + 6	0 + 7	0 + 8	0 + 9	0 + 10
1	1 + 0	1 + 1	1 + 2	1 + 3	1 + 4	1 + 5	1 + 6	1 + 7	1 + 8	1 + 9	1 + 10
2	2 + 0	2 + 1	2 + 2	2 + 3	2 + 4	2 + 5	2 + 6	2 + 7	2 + 8	2 + 9	2 + 10
3	3 + 0	3 + 1	3 + 2	3 + 3	3 + 4	3 + 5	3 + 6	3 + 7	3 + 8	3 + 9	3 + 10
4	4 + 0	4 + 1	4 + 2	4 + 3	4 + 4	4 + 5	4 + 6	4 + 7	4 + 8	4 + 9	4 + 10
5	5 + 0	5 + 1	5 + 2	5 + 3	5 + 4	5 + 5	5 + 6	5 + 7	5 + 8	5 + 9	5 + 10
6	6 + 0	6 + 1	6 + 2	6 + 3	6 + 4	6 + 5	6 + 6	6 + 7	6 + 8	6 + 9	6 + 10
7	7 + 0	7 + 1	7 + 2	7 + 3	7 + 4	7 + 5	7 + 6	7 + 7	7 + 8	7 + 9	7 + 10
8	8 + 0	8 + 1	8 + 2	8 + 3	8 + 4	8 + 5	8 + 6	8 + 7	8 + 8	8 + 9	8 + 10
9	9 + 0	9 + 1	9 + 2	9 + 3	9 + 4	9 + 5	9 + 6	9 + 7	9 + 8	9 + 9	9 + 10
10	10 + 0	10 + 1	10 + 2	10 + 3	10 + 4	10 + 5	10 + 6	10 + 7	10 + 8	10 + 9	10 + 10

Children will also need to recall the inverse subtraction fact. All of the above facts should be instantly recalled by children by the end of Year 2. A blank copy is kept in the back of maths books, so when children are secure with the facts, this can be highlighted with the relevant colour for that term.

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All children should be secure in these facts when leaving the year group:

EYFS

- Recognise the number 0-20
- Know one more and 1 less for number 0-20
- Know the days of the week in order
- Identify 2D shapes: circle, square, triangle, rectangle, hexagon, pentagon
- Identify 3D shapes: sphere, cylinder, cone, cubes, cuboids

Year 1

- Facts within 10 as above and related subtraction facts
- Know o'clock and half past times
- Know the seasons in order
- Know the months of the year in order
- Identify 3D shapes: pyramids, square based pyramids

Year 2

- Facts within 20 as above and related subtraction facts
- Doubles and halves of numbers to 20
- Multiplication and division facts 2, 5 and 10 x tables
- Know quarter past and quarter to times, as well as intervals of 5
- Number of minutes in an hour; number of hours in a day
- Coin recognition up to £2 and note recognition
- Know 100p=£1
- Identify 2D shapes: quadrilaterals, regular and irregular polygons
- Identify 3D shapes: cuboids, prisms



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Year 3

- Sums and differences between pairs of numbers which are multiples of 10 and 100
- Doubles and halves of multiples of 10 or 100
- Complements to 100
- Complements to 60 (time)
- Complements of fractions with the same denominator that make 1 e.g. $\frac{3}{7} + \frac{4}{7} = 1$
- $\times 3$, $\times 4$, $\times 8$ facts including division facts
- Number of seconds in a minute, number of minutes in an hour, number of hours in a day, number of days in a week
- Number of days in each month and in a year including a leap year
- Recognise right angles
- Recognise parallel and perpendicular lines
- Recognise horizontal and vertical

Year 4

- Review addition and subtraction facts within 20, ensure application to 10, 100 and 1000 ($6 + 3$, $60 + 30$, $600 + 300$, $6000 + 3000$)
- Doubles and halves of multiples of 10, 100 or 1000 ($6 + 6$, $60 + 60$, $600 + 600$, $6000 + 6000$)
- All multiplication and division facts to 12×12
- Multiplication and division by zero and one facts
- Division and multiplication by 10 and 100
- Conversion of kilometres to metres, hours to minutes, years to months, weeks to days
- Complements of tenths that make 1
- Complements of hundredths that make 1
- Convert between decimals and fractions for $\frac{1}{2}$, $\frac{1}{4}$, $\frac{3}{4}$ and any number of tenths and hundredths
- Read Roman Numerals to 100
- Know right angles = 90 degrees
- Know the types of triangle (isosceles, equilateral, scalene)

Year 5

- Identify prime numbers up to 20 (2, 3, 5, 7, 11, 13, 17, 19)
- Recall metric conversions (1 kilogram = 1000 grams, 1 kilometre = 1000 metres, 1 metre = 100 centimetres, 1 metre = 1000 millimetres, 1 centimetre = 10 millimetres 1 litre = 1000 millilitres)
- Recall square numbers up to 12 squared and their square roots



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- Read Roman Numerals to 1000
- Know angles on a straight line = 180 degrees
- Know angles in a triangle = 180 degrees
- Know angles around a point = 360 degrees

Year 6

1/2	0.5	50%
1/4	0.25	25%
3/4	0.75	75%
1/5	0.2	20%
1/10	0.1	10%
2/5	0.4	40%
1/100	0.01	1%
9/100	0.09	9%
21/100	0.21	21%
1/20	0.05	5%

- Convert between decimals, fractions and percentages
- Identify prime numbers up to 50 (2, 3, 5, 7, 11, 13, 17, 19, 23, 27, 29, 31, 37, 41, 43, 47)
- Illustrate and name parts of a circle, including radius, diameter and circumference and know that the diameter is twice the radius



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